We present an analysis of the decay $D^0 \rightarrow K^+ \pi^-$ from FOCUS. From a sample of 234 events we find a branching ratio of $\frac{\Gamma(D^0 \rightarrow K^+ \pi^-)}{\Gamma(D^0 \rightarrow K^- \pi^+)} = (0.430 \pm 0.062 \pm 0.031)\%$ under the assumption of no mixing and no CP violation. We also present limits on charm mixing.

1. Introduction and event selection

Charm mixing remains elusive. In the Standard Model the charm mixing rate is greatly suppressed by small CKM matrix elements and strong GIM suppression. This very fact, however, provides a unique opportunity to search for new physics.

The search for charm mixing requires tagging the flavor of a neutral charm meson at production and again tagging the flavor at decay. The production flavor is determined using $D^+ \rightarrow D^0 \pi^+$ decays. The decay flavor is determined by reconstructing a Cabibbo favored (CF) decay with a charged kaon such as $D^0 \rightarrow K^- \pi^+$. A right-sign (RS) decay is defined as one in which the kaon and soft pion charges are opposite while same kaon and $\pi_s$ charges are wrong-sign (WS) decays. The $D^0$ can also decay directly to $K^+ \pi^-$ via a doubly Cabibbo suppressed decay (DCSD).

The time dependent WS decay rate can be written as:

$$R_{WS}(t) = e^{-\Gamma t} \left( R_D + \sqrt{R_D y} \Gamma t + \frac{1}{4} \left( x'^2 + y'^2 \right) \Gamma^2 t^2 \right)$$

where the three terms correspond to DCSD, interference between mixing and DCSD, and mixing. $R_D$ is the DCS branching ratio relative to the Cabibbo favored mode. The parameters $x' \equiv x \cos \delta_{K\pi} + y \sin \delta_{K\pi}$ and $y' \equiv y \cos \delta_{K\pi} - x \sin \delta_{K\pi}$ are rotated versions of the mixing parameters $x \equiv \frac{\Delta M}{\Gamma}$ and $y \equiv \frac{\Delta \Gamma}{2 \Gamma}$ (mass and lifetime splitting terms) and $\delta_{K\pi}$ is the strong phase between CF and DCS decay. Discovery of hadronic charm mixing requires separating the three components of Eq. 1 using the different lifetime distributions. Note that Eq. 1 has no information on the sign of $x'$ and therefore the relevant fit variable is $x'^2$. In this analysis, CP violation effects are not considered and charge conjugates are implied.

FOCUS recorded data during the 1996–7 fixed-target run at Fermilab. A photon beam impinged on BeO targets. 16 silicon strip planes provide vertexing and track-
ing. Charged particles are tracked and momentum analyzed as they pass through up to two dipole magnets and up to five sets of multiwire proportional chambers. Three Čerenkov counters, two EM calorimeters, and two muon detectors identify particles. A candidate driven vertexing algorithm is used to reconstruct charm. For $D^0 \rightarrow K^- \pi^+$, two tracks must verticize with CL > 2%. This candidate is used to seed the production vertex which must have CL > 1%. The soft pion $\pi^+$ from the $D^{*+} \rightarrow D^0 \pi^+$ must be consistent with originating from the production vertex and the track is refit to the production vertex. Separating charm from hadronic background is primarily accomplished by requiring the decay vertex be distinct from the production vertex. Other cuts are made to ensure the vertex is isolated and is more charm like than background like. Strong Čerenkov cuts are applied to the combination of $K^-$ and $\pi^+$ especially if the invariant mass under a reflection of $K^- \rightarrow \pi^-$ and $\pi^+ \rightarrow K^+$ is close to the $D^0$ mass. If more than one $D^{*+}$ candidate is found for one $D^0$ candidate an additional cut may be made. If a RS (WS) candidate is found with $2.5 \text{ MeV} < Q(D^*) < 9.5 \text{ MeV}$ then no WS (RS) candidates are allowed.

2. Fit description and results

A 3D binned maximum likelihood fit is used in this analysis. Two dimensions, $M(D^0)$ and $Q(D^*)$ separate signal from background while $\tau(D^0)$ distinguishes DCSD, mixing, and interference. The fit components generally have a shape determined by a Monte Carlo simulation and a yield which is free to float, some with weak constraints imposed. The components making up the fit which are modeled by the Monte Carlo are RS signal, WS signal (DCSD, interference, and mixing), real $D^0 \rightarrow K^- \pi^+$ decay with a fake soft pion. reflections to both RS and WS ($K^- K^+, \pi^- \pi^+, \pi^- \pi^+ \pi^0$, $K^0 \pi^- \pi^+$), RS background ($K^- \ell^+ \nu$ and $K^- \pi^+ \pi^0$), and WS background (double misidentification of $K^- \ell^+ \nu$, $K^- \pi^+ \pi^0$, $K^- \pi^+$). The remaining background is some combination of non-charm and poorly reconstructed charm events. This is modeled with functional forms in mass $a \exp(-bm)$, energy release $\alpha q^{1/2} + \beta q^{3/2}$, and lifetime $\exp(-t/\tau_1) + \eta \exp(-t/\tau_2)$. Penalty terms are added to ensure backgrounds are consistent with known branching ratios. The affected backgrounds are the $D^0$ decays to $K^+ K^-, \pi^+ \pi^-, \pi^+ \pi^- \pi^0$, $K^0 \pi^+ \pi^-$, $K^- \pi^+ \pi^0$, and $K^- \ell^+ \nu$ which all appear in RS and WS. The background due to double misid of the RS signal is fixed based on the RS yield and relative efficiency.

Mini Monte Carlo tests of the fit were used to verify the accuracy of the reported fit errors and to check for possible biases in the fit. No significant bias was found and the reported fit errors agree with the mini Monte Carlo results. Fit variants with different binning, different constraints, and different accounting of the random background were tried. No significant differences were observed. Variations of all the selection criteria were also analyzed with no significant differences in the results. For the branching ratios reported, systematic errors due to fit variants and cut variants were obtained from the r.m.s of the variations and then added in quadrature.
Fitting without mixing we find $R_{WS} = (0.430^{+0.062}_{-0.061} \pm 0.031)\%$. From the standard mixing fit we find a DCS branching ratio of $R_D = (0.382^{+0.166}_{-0.165} \pm 0.069)\%$. Figure 1 shows the WS projections onto $M(D^0)$ and $Q(D^\prime)$. The RS data is dominated by 54452 ± 242 signal events. Due to significant correlations between $x'$ and $y'$, the interesting physics result is a contour in the $x', y'$ plane. Although we fit for $x'^2$, we choose to plot $x'$. The 95% CL contour is defined as the location in the $x', y'$ plane where $\Delta \log L = 2.996$ relative to the minimum $-\log L$ in the physical region of the $x', y'$ plane. While the true minimum occurs at $x'^2 = -0.06\%$ and $y' = 1.0\%$, the minimum with $x'^2 \geq 0$ occurs at $x'^2 = 0$ and $y' = 0.5\%$ with a change in $-\log L$ of only 0.006 relative to the true minimum. Systematic checks were performed with 120 fit and cut variants. The contour variation is consistent with differences in the returned value of $x'^2$ and $y'$. For the systematic error, we first find the change in $-\log L$ between the global minimum and the $x', y'$ location for each of the variants. We then find the value greater than 95% of these differences which is 0.482. We find the contour at which the change in $-\log L$ is 2.996 + 0.482 = 3.478 and call this the 95% CL including systematic error. The $\tau(D^0)$ projection and $x', y'$ contours are shown in Fig. 1. Defining 95% CL limits on $x'$ and $y'$ based on the projection of the contour onto the respective axis we find $x'^2 < 0.83\%$ and $7.2\% < y' < 4.1\%$. 

Fig. 1. The top plots show projections onto $M(D^0)$ and $Q(D^\prime)$ of the fit and data for WS events. The bottom-left plot shows the contributions to the WS signal versus $\tau(D^0)$. The bottom-right plots shows the 95% CL $x', y'$ contour with statistical (inner) and full errors (outer).

Hadronic charm mixing results from FOCUS 3