

# LSD SU(3) $N_f=8$ Project

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for the  
Lattice Strong Dynamics (LSD) Collaboration

Lattice for Beyond the Standard Model Physics  
Boulder, Colorado  
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# Can the Higgs Boson be Composite?

- From the LHC we have learned that the Standard Model has a Higgs boson whose mass is half as large as the VEV of the Higgs field.
- A minimal  $SU(2) \times SU(2) \sim O(4)$  linear sigma model (LSM) for the Higgs sector works quite well for calculational purposes but is confusing as it seems renormalizable to high scales but also fine tuned.
- We can imagine the Higgs sector is composite and the LSM is part of a low-energy EFT but experiment currently gives us little guidance as to the breakdown scale of the EFT or even all the relevant degrees of freedom (dof) of the EFT.
- $SU(3) N_f=2$  (QCD) is an example composite theory that has just the right low energy dof for composite Higgs, but the mass is four times the VEV.
- So, if the Higgs is composite it is probably embedded in a larger EFT than the  $O(4)$  LSM.

# Requirements for Composite Higgs

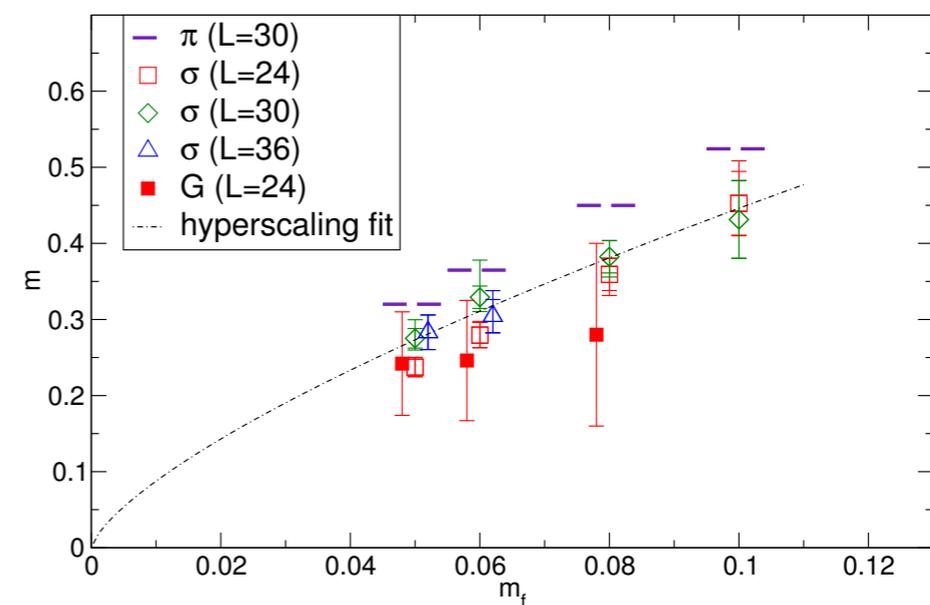
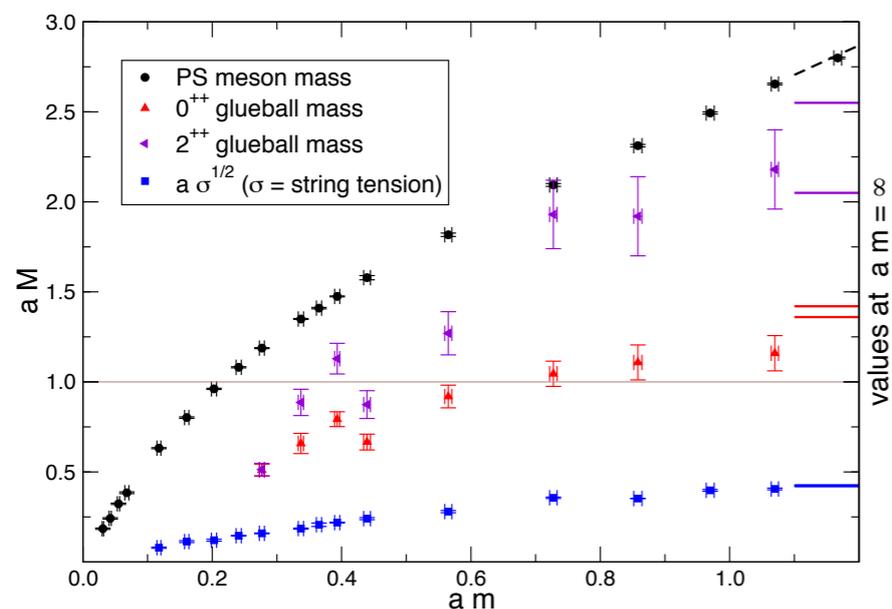
- If a gauge theory with 3 or more NG bosons is to be a candidate for a composite Higgs theory, it should pass a few tests (order of difficulty):
  1. The Higgs boson should have a mass about half the VEV in the chiral limit.
  2. If there are more than three NG bosons, can the rest be given a modest mass while keeping the Higgs mass light?
  3. Below the mass scale of the extra NG bosons (and other hadrons) does a  $SU(2) \times SU(2)$  LSM emerge?
  4. If the Higgs is to be composite, how does the Yukawa mechanism work? How are FCNC suppressed?
- Extra hadrons are not necessarily a problem, *e.g.* if the 750 GeV diphoton or 2 TeV diboson resonances had been confirmed, they could be accommodated in these models as an  $\eta$  or  $\rho$  meson.

# Theories with Light Scalars

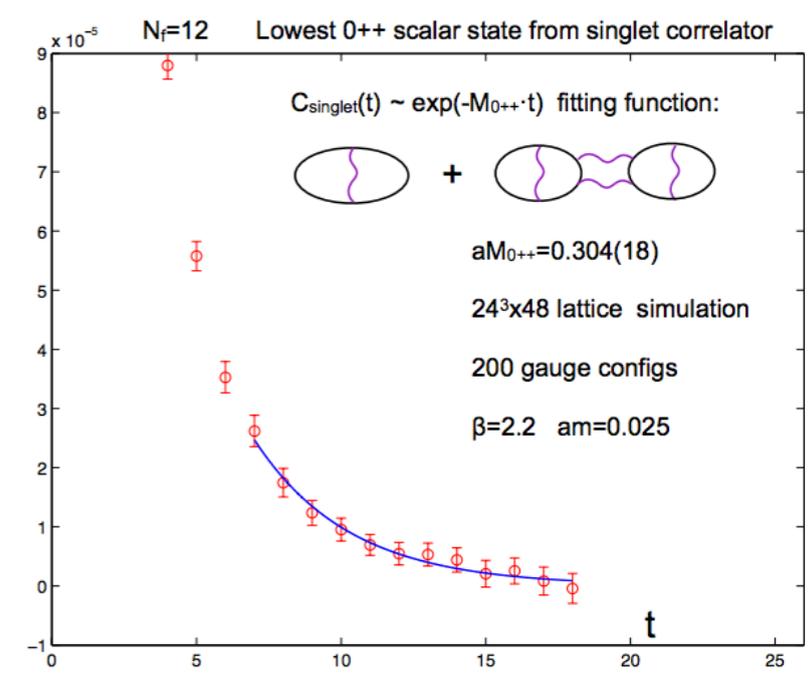
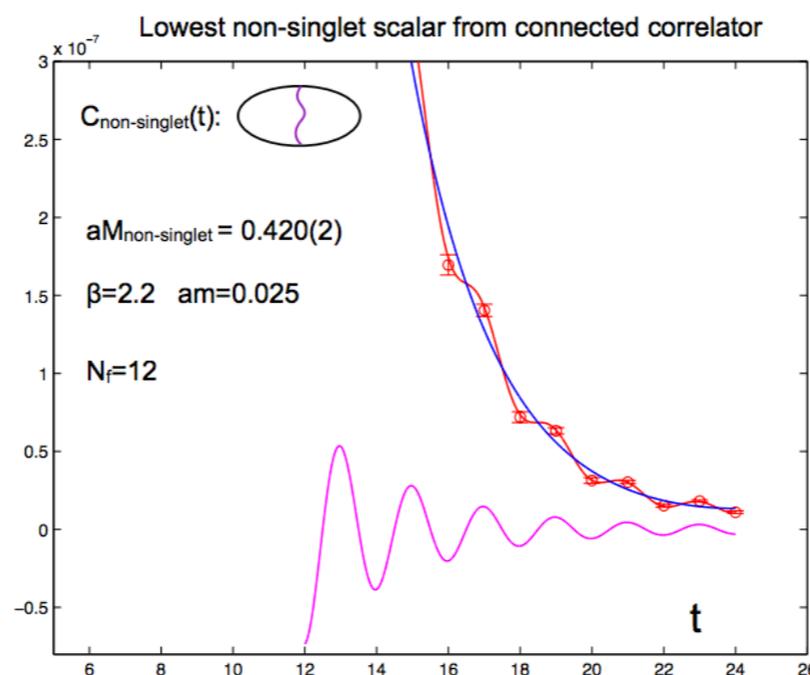
- Mass-deformed IRFP theories with very light scalars.

SU(2)  $N_f=2$  adj (Edinburgh)  
 Phys. Rev. D 82, 014510 (2010)

SU(3)  $N_f=12$  fund (LatKMI)  
 Phys. Rev. Lett. 111, 162001 (2013)



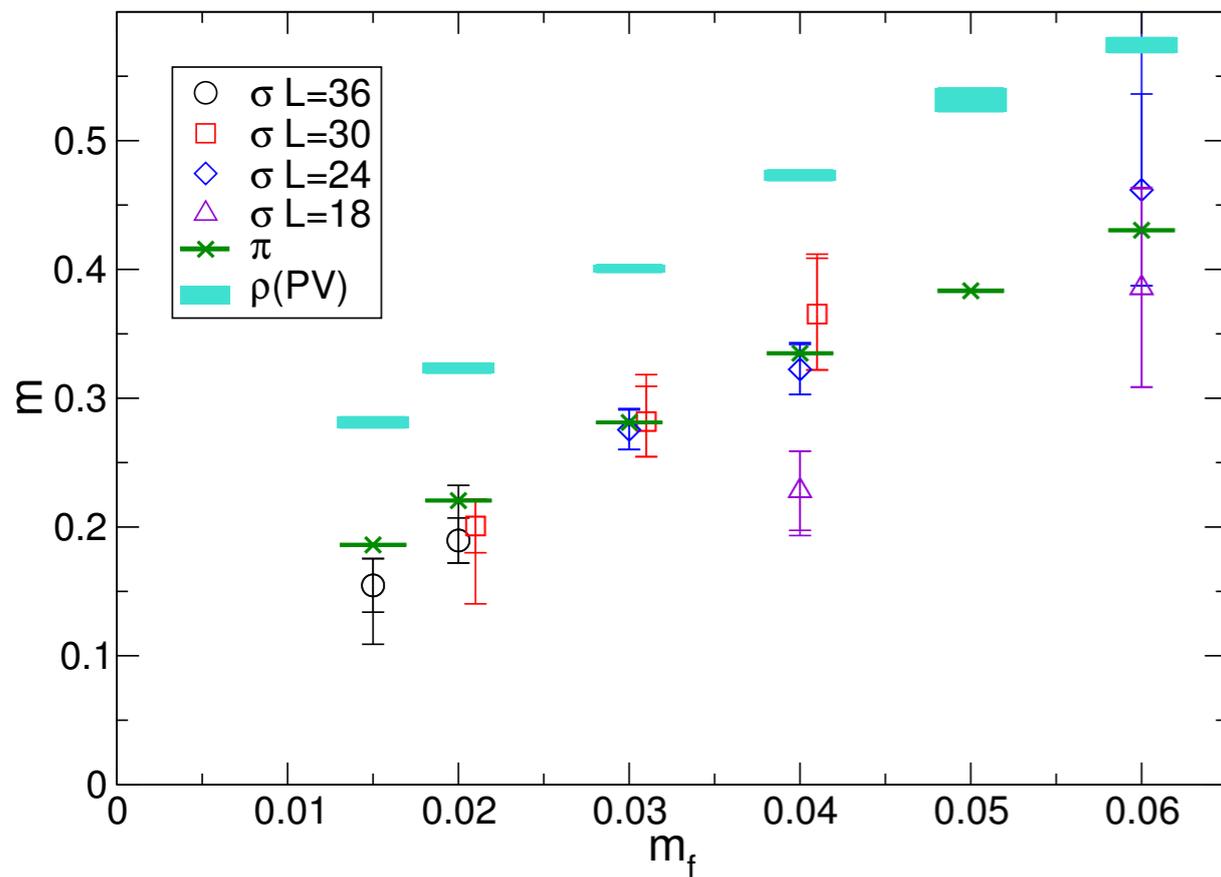
SU(3)  $N_f=12$  fund (LatHC)  
 USQCD White Paper 2013



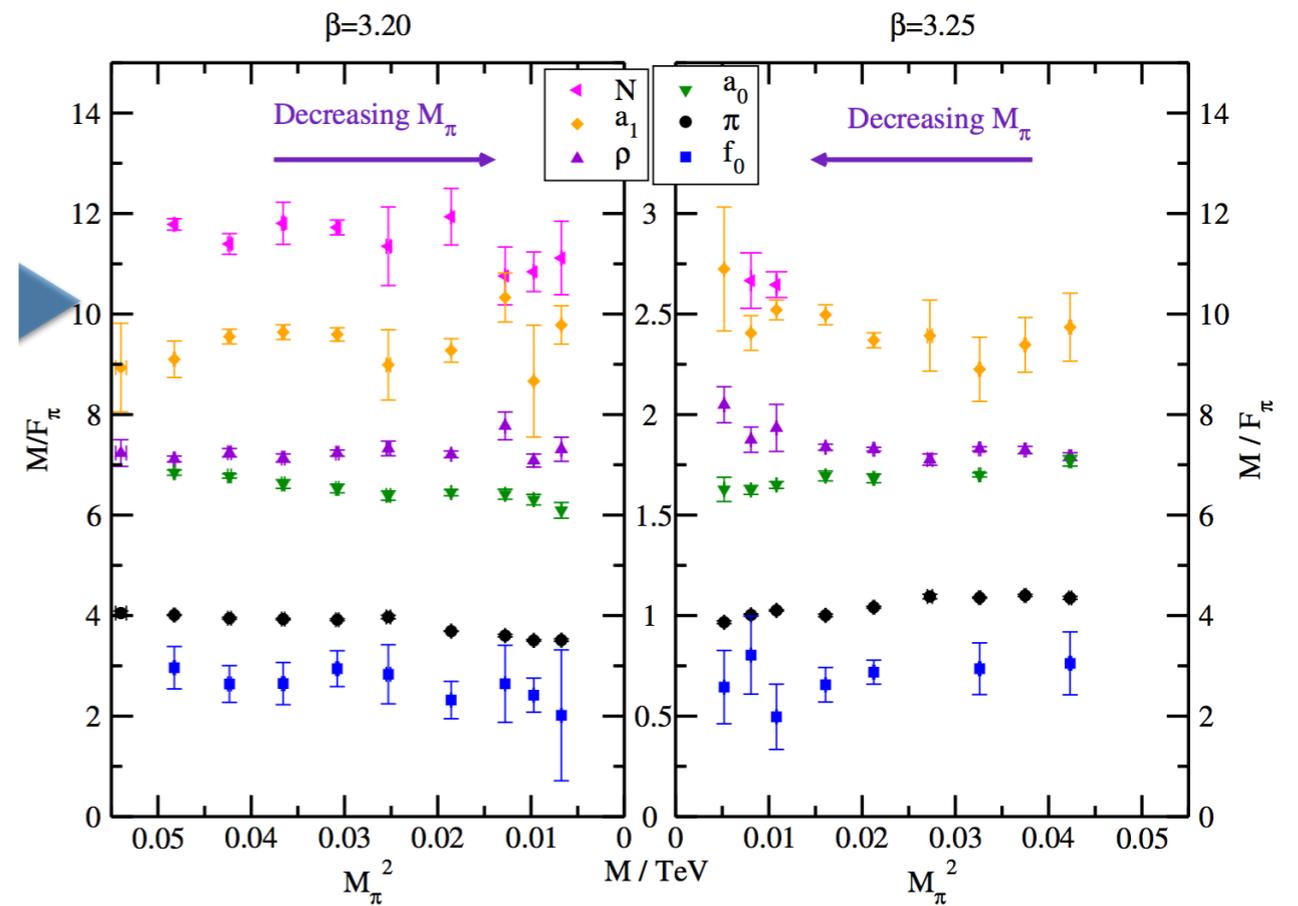
# More Light Scalars

- Theories likely just outside conformal window also have light scalars.

SU(3)  $N_f=8$  fund  
 LatKMI (Nagoya)  
 Phys. Rev. D 89, 111502 (2014)



SU(3)  $N_f=2$  sym  
 LatHC Collaboration  
 LATTICE 2015



★ light  
 ■ heavy

# SUMMARY RESULTS

SU(3)  
 N<sub>f</sub>=2 (S)

## Template Models

## Scalar

SU(2) N<sub>f</sub>=2 (F)



SU(2) N<sub>f</sub>=2 (A)



SU(2) N<sub>f</sub>=1 (A)



SU(3) N<sub>f</sub>=12 (F)



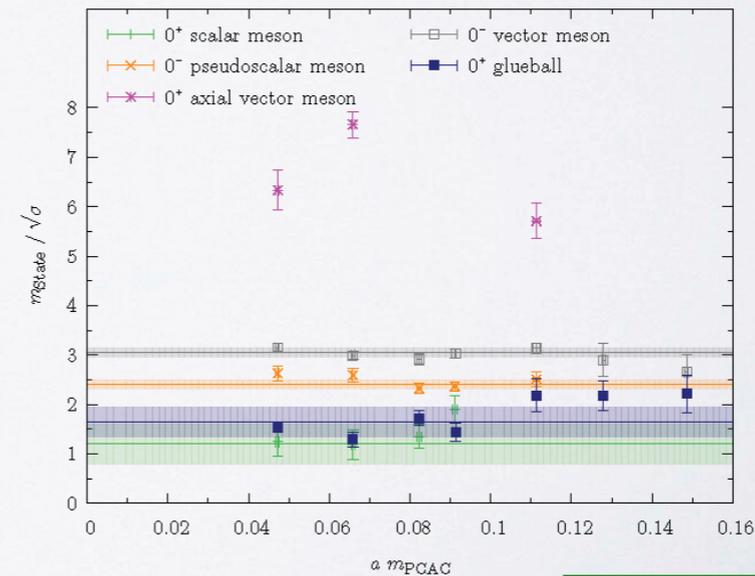
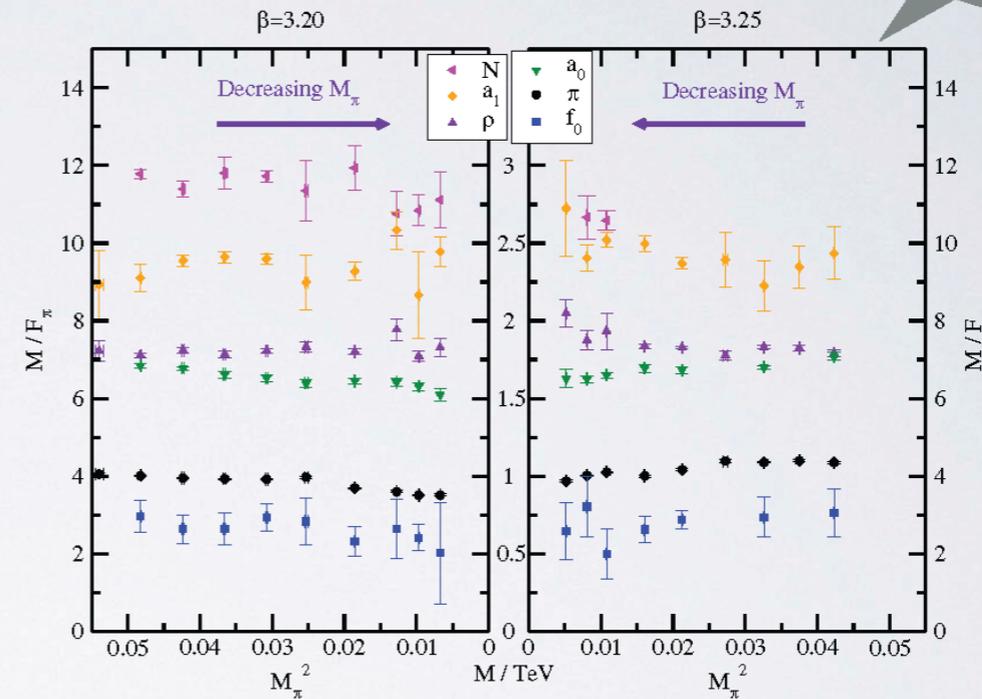
LSD → SU(3) N<sub>f</sub>=8 (F)



SU(3) N<sub>f</sub>=4 (F)



SU(3) N<sub>f</sub>=2 (S)



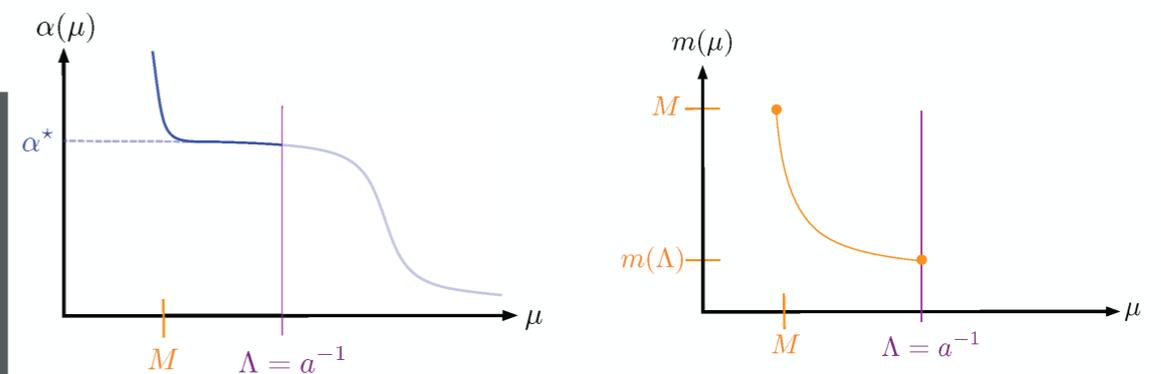
SU(2)  
 N<sub>f</sub>=1 (A)

**E. Rinaldi**

# Confinement vs. Mass-Deformed IRFP

- Confinement is induced in mass-deformed IRFP at scale where fermions decouple
- Theory is IR Conformal if  $M \rightarrow 0$  as  $m \rightarrow 0$ .
- In walking theory, another scale  $\Lambda_c$  should emerge.
- Technical challenge in walking theory on lattice is to have physically big enough volume that  $M \ll \Lambda_c$ .
- Typically  $M \sim \Lambda_c$  so it's difficult to conclude whether  $\Lambda_c$  exists.

## Mass deformation of IR CFT



- “Seed mass” at high scale runs into the IR

$$m(\mu) = m(\Lambda) \left( \frac{\Lambda}{\mu} \right)^{\gamma^*}$$

- Fermions screen out, theory confines at  $M$

$$M \sim m^{1/(1+\gamma^*)}$$

- Confinement scale depends on  $m$ , governed by anomalous mass dimension at fixed point

All hadron masses scale  $\sim M$

# Analytic Musings (I)

## Why the Higgs boson might be a pseudo-dilaton

- Since 1980's, theorists have wondered whether Nambu-Goldstone theorem applies to quasi-scale invariant theories producing light pseudo-dilaton. [Bardeen, Leung, Love ('86); Yamawaki, Bando, Matumoto ('86); Holdom, Terning ('88); Gusynin, Miransky ('88); Dietrich, Sannino, Tuominen ('05); Appelquist, Bai ('10); Vecchi ('10)]
- There exists a perturbative model of a parametrically-light pseudo-dilaton as a proof of principle [B. Grinstein, P. Uttayarat ('10)]. Importantly, they matched the IR of this theory to a dilaton EFT [Goldberger, Grinstein, Skiba ('08)].
- The dilaton EFT is strikingly similar to the Higgs sector of the Standard Model, so the Higgs boson could be a pseudo-dilaton.

# Quasi-conformality, fermion mass generation and FCNC

- Walking gauge theories were originally proposed to solve a problem with fermion mass generation and FCNC in Extended Technicolor (ETC) [Holdom ('81); Holdom ('85); Akiba, Yanagida ('86)].
- It was quickly conjectured that a light dilaton might also appear in walking technicolor [Yamawaki, Bando, Matumoto ('86)].

- Related discussion by Sannino earlier today.

- In extended technicolor (ETC)<sup>1</sup>, masses and FCNC's from

$$\text{Masses : } \frac{(\bar{Q}Q)(\bar{q}q)}{\Lambda_{\text{ETC}}^2} \quad \text{FCNC's : } \frac{(\bar{q}q)(\bar{q}q)}{\Lambda_{\text{ETC}}^2}$$

- For current limits on FCNC's involving strange quarks

$$\Lambda_{\text{ETC}} \gtrsim 1000 \text{ TeV}$$

- So, the natural scale for strange quark mass in ETC

$$m_s \sim \langle \bar{Q}Q \rangle / \Lambda_{\text{ETC}}^2$$

- In QCD  $\langle \bar{\psi}\psi \rangle \sim (3f_\pi)^3$ , so in QCD-like TC ( $v \sim 246 \text{ GeV}$ )

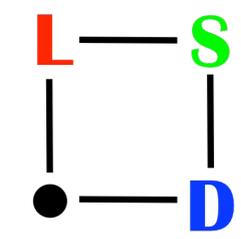
$$\langle \bar{Q}Q \rangle \sim (3v)^3 \sim (750 \text{ GeV})^3 \implies m_s \sim 0.4 \text{ MeV}$$

- Conjectured walking mechanism may provide enhancement

$$\langle \bar{Q}Q \rangle \sim (3v)^2 \Lambda_{\text{ETC}} \implies m_s \sim 63 \text{ MeV}$$

- Generating top quark masses a serious challenge for ETC.

<sup>1</sup>T. Appelquist, M. Piai, R. Shrock, Phys. Rev. D **69**,105002 (2004) 



# Lattice Strong Dynamics Collaboration



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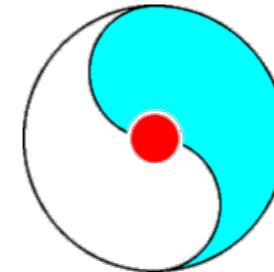
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Richard Brower  
Claudio Rebbi  
Evan Weinberg



Oliver Witzel



Tom Appelquist  
George Fleming  
Andy Gasbarro



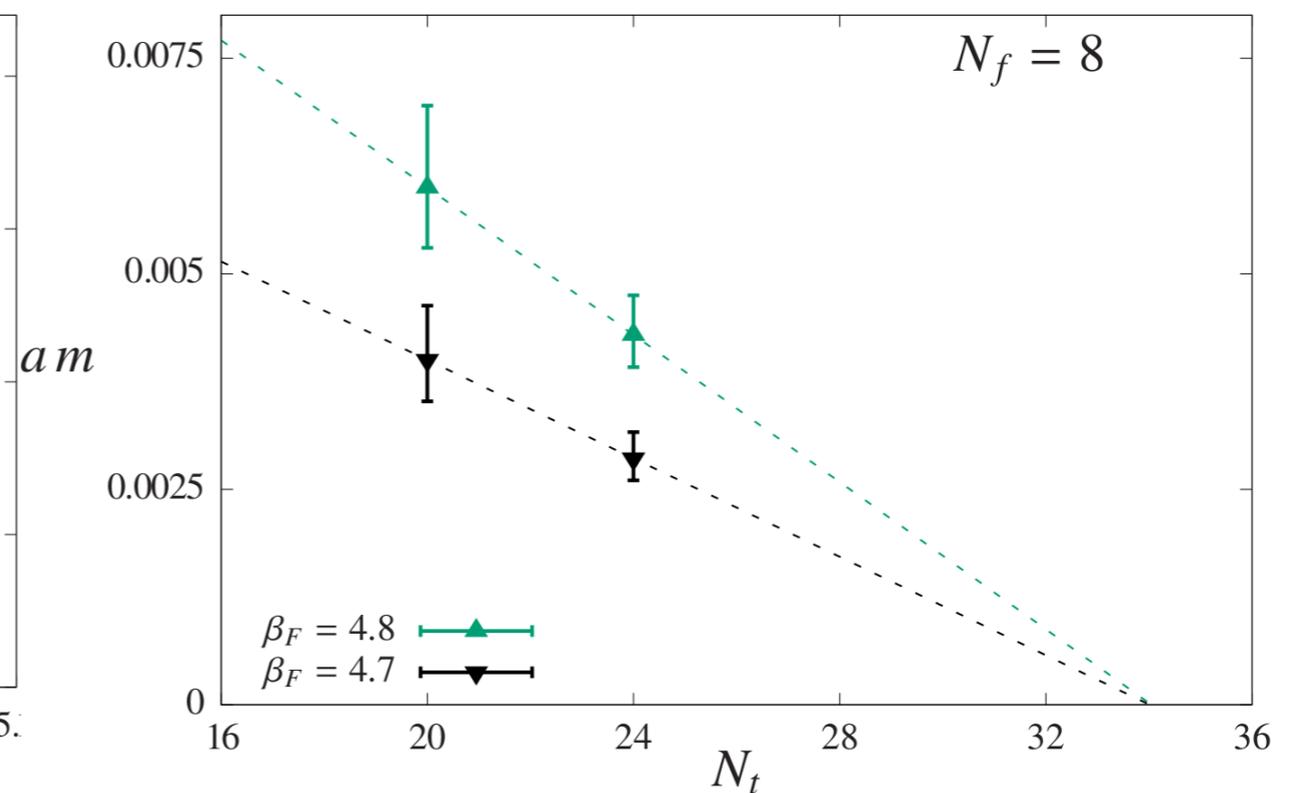
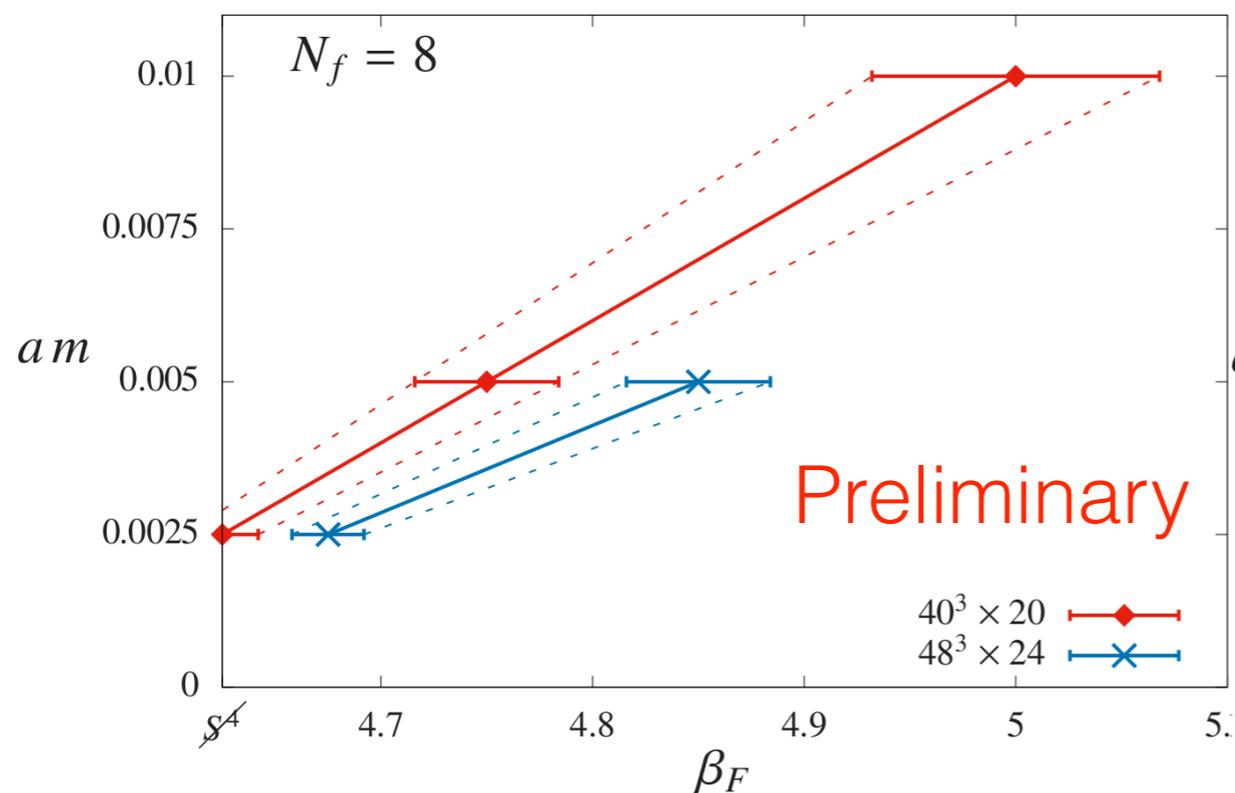
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Pavlos Vranas

# LSD SU(3) $N_f=8$ Stag

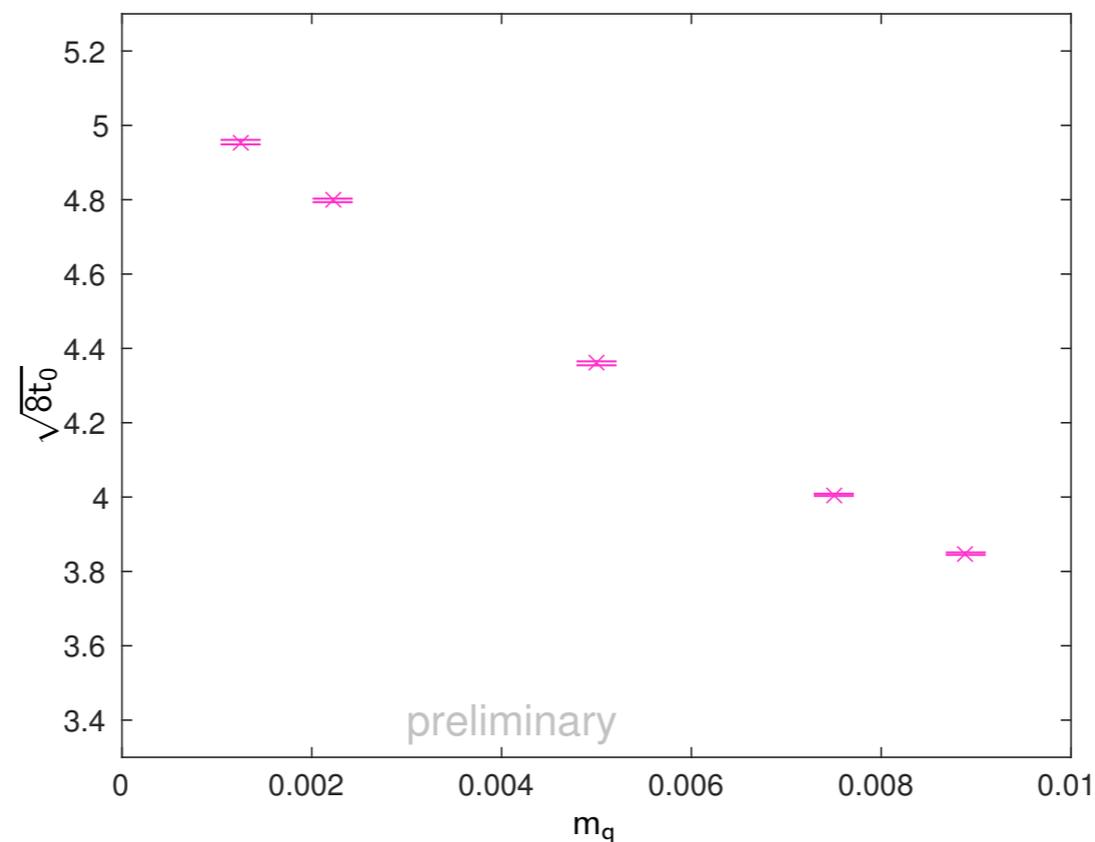
- Earlier USBSM studies (and LatKMI) used HISQ fermions which become prohibitively expensive for  $N_f=8$  on coarse lattices.
- Using nHYP stag fermions and fund+adj gauge action pioneered by Boulder group to get to somewhat coarser (but still very fine) lattices.



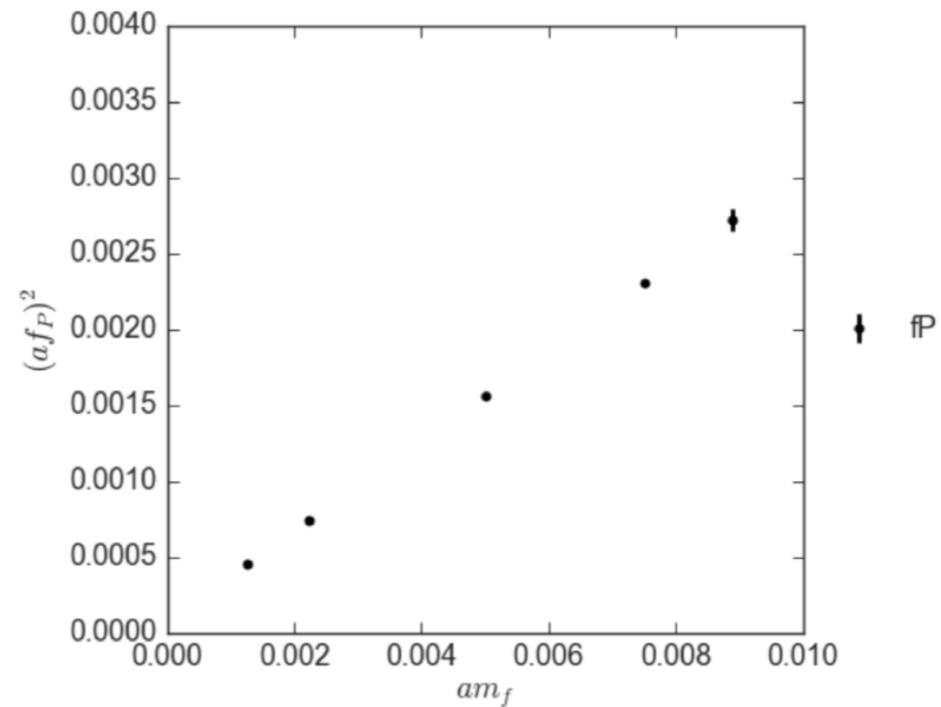
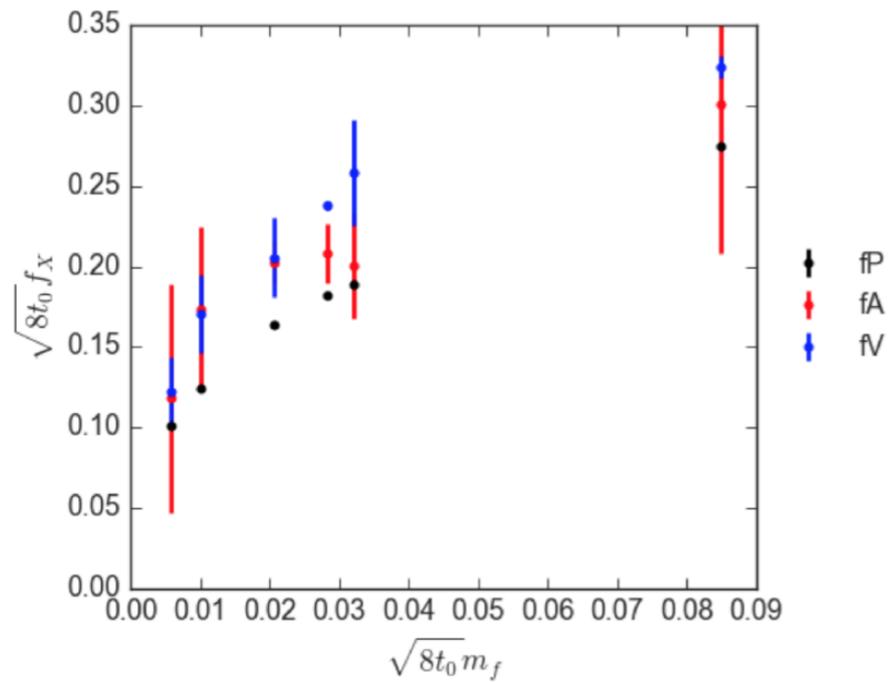
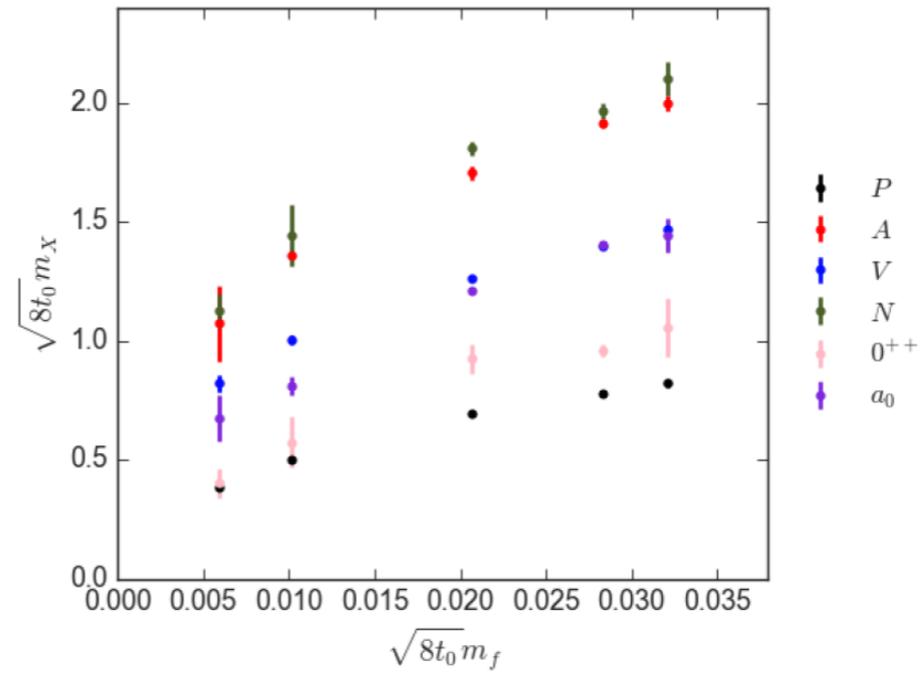
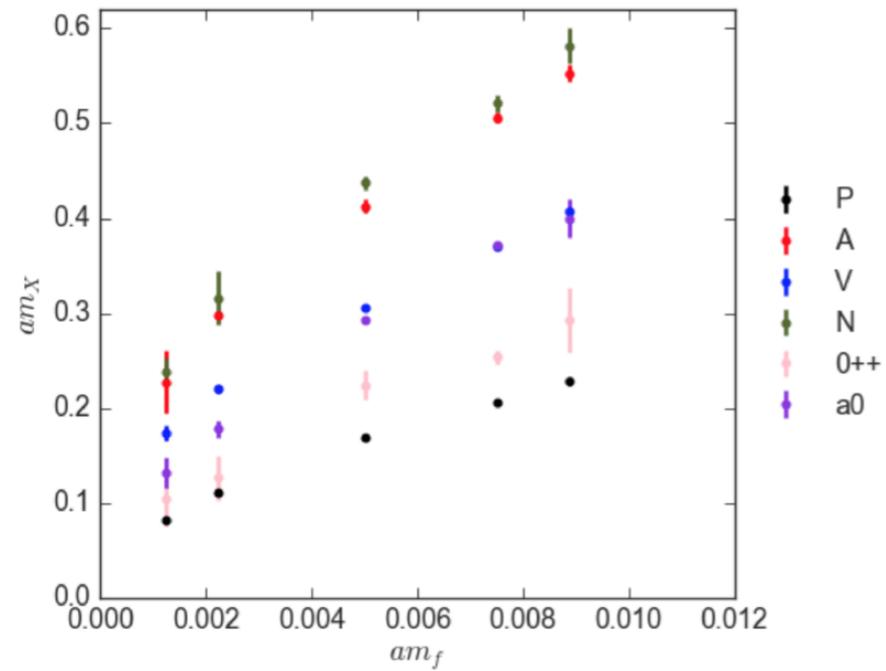
$T_c$  and bulk phase

# Near Conformal Scale Setting

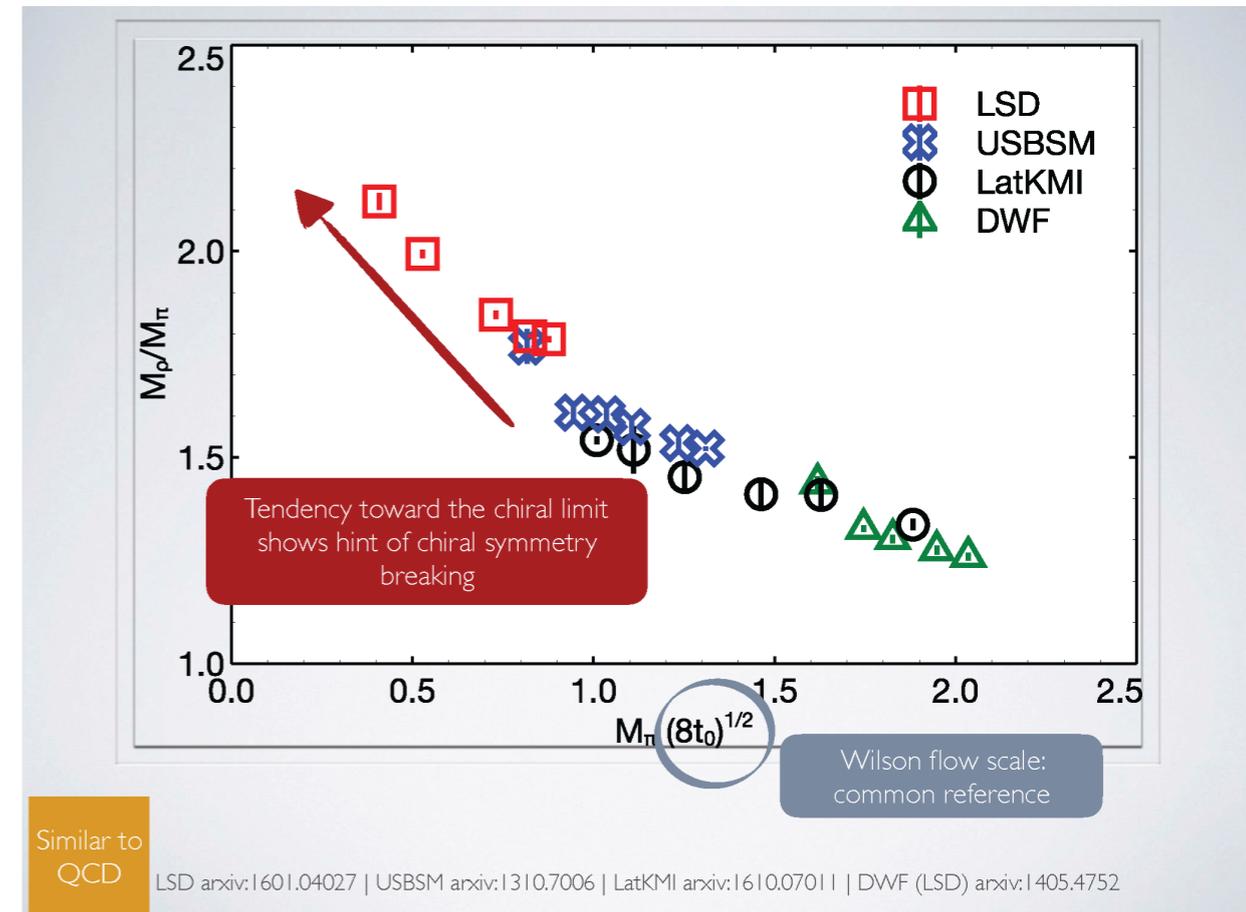
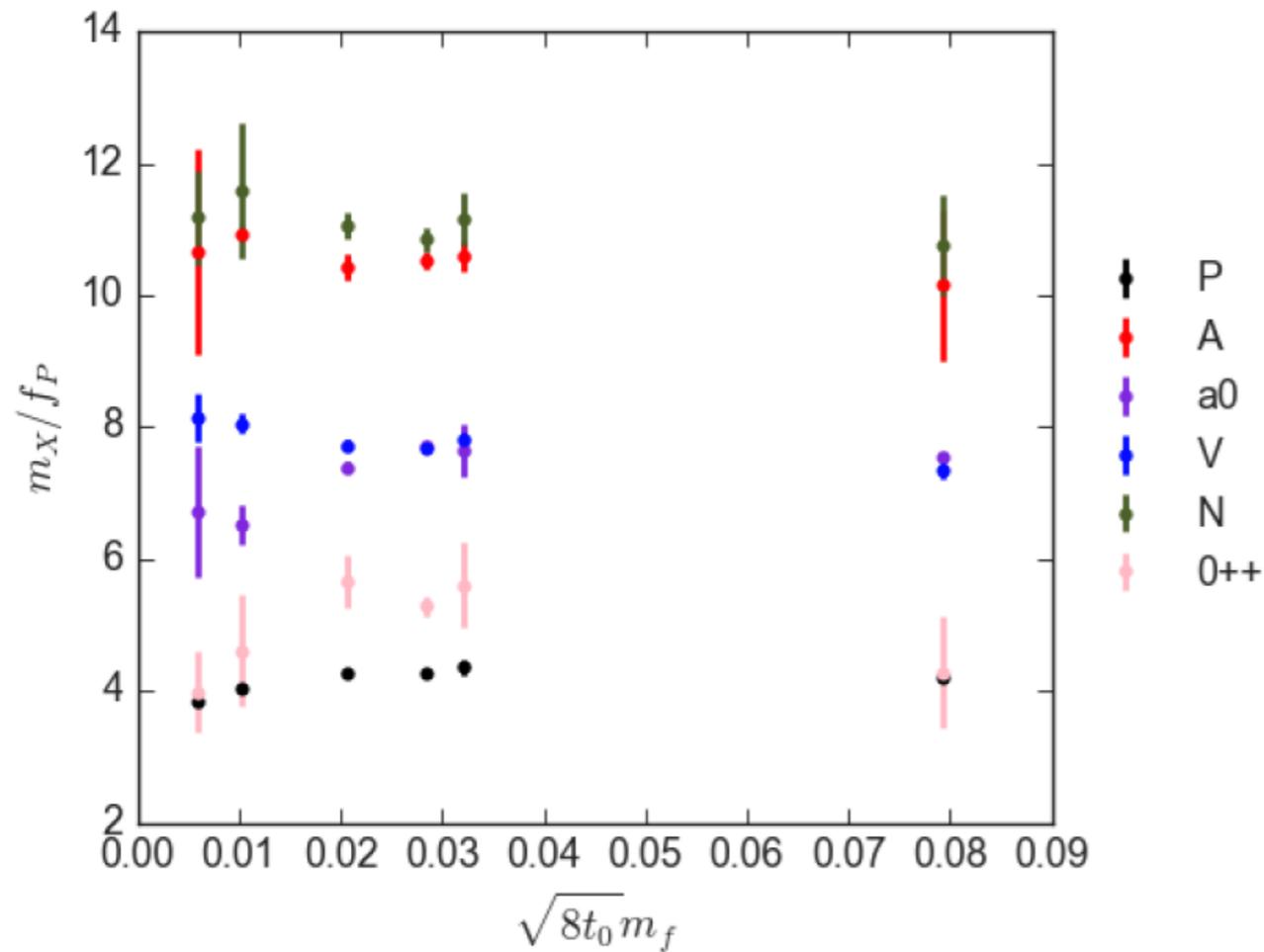
- In QCD, the dynamical scale  $a^{-1}$  is strongly affected by gauge coupling and weakly affected by quark mass.
- This reflects strong gluonic anti-screening and weak fermionic screening in vacuum.
- Near conformal dynamics has balanced anti-screening and screening, leading to strong mass dependence in setting the scale



# Hadron Spectrum



# Hyperscaling of Mass-Deformed IRFP?



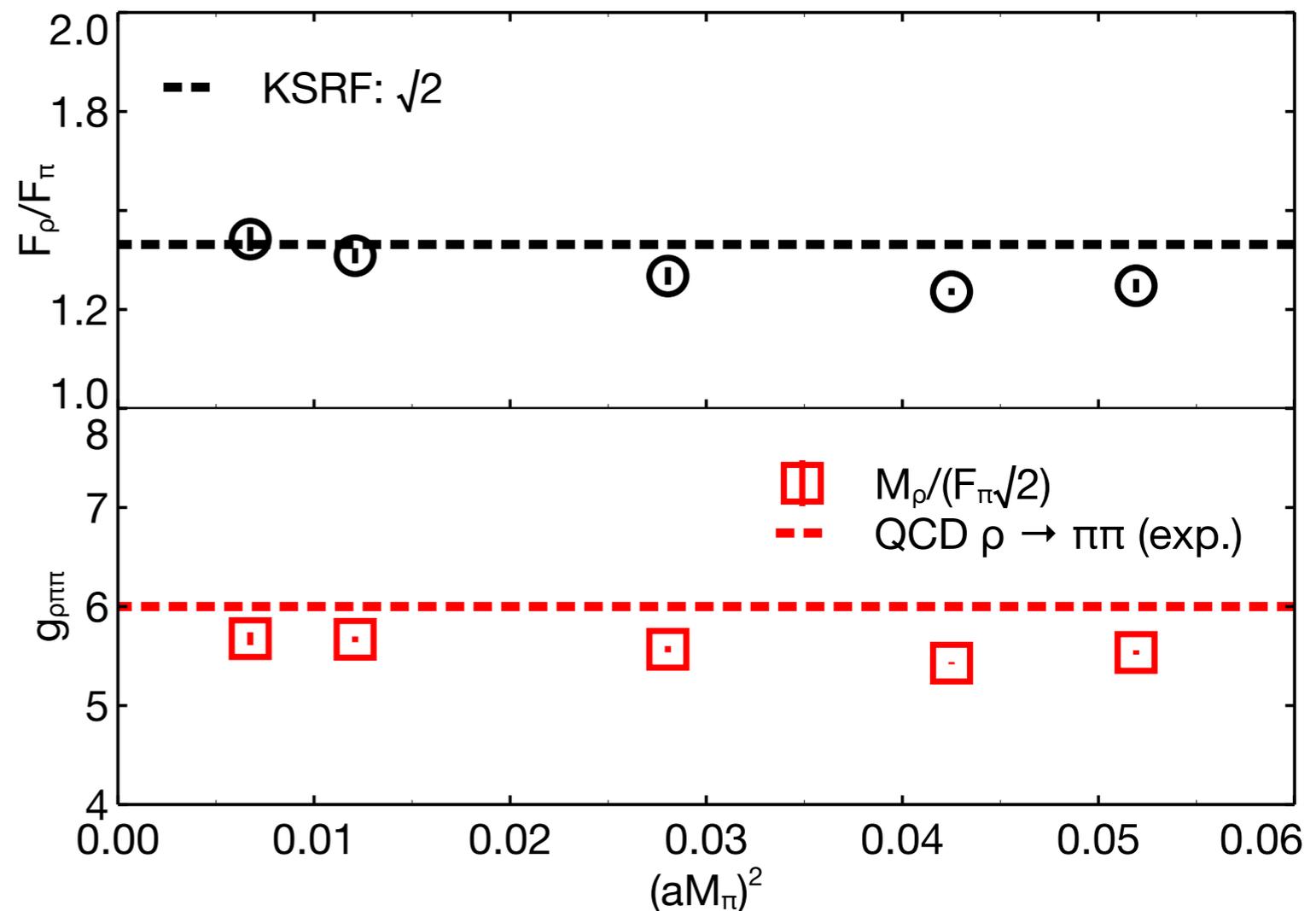
**E. Rinaldi**

# KSRF Relation

- Dynamical origin of vector meson dominance (VMD) not well understood in QCD. Is it also true in  $N_f=8$ ?
- Seems to be true, so in LHC might expect 2 TeV vector resonances with  $\sim 25\%$  width.

$$F_\rho = \sqrt{2} F_\pi, \quad g_{\rho\pi\pi} = \frac{M_\rho}{\sqrt{2} F_\pi},$$

$$\Gamma_\rho \approx \frac{g_{\rho\pi\pi}^2 M_\rho}{48\pi} \approx \frac{M_\rho^3}{96\pi F_\pi^2}$$



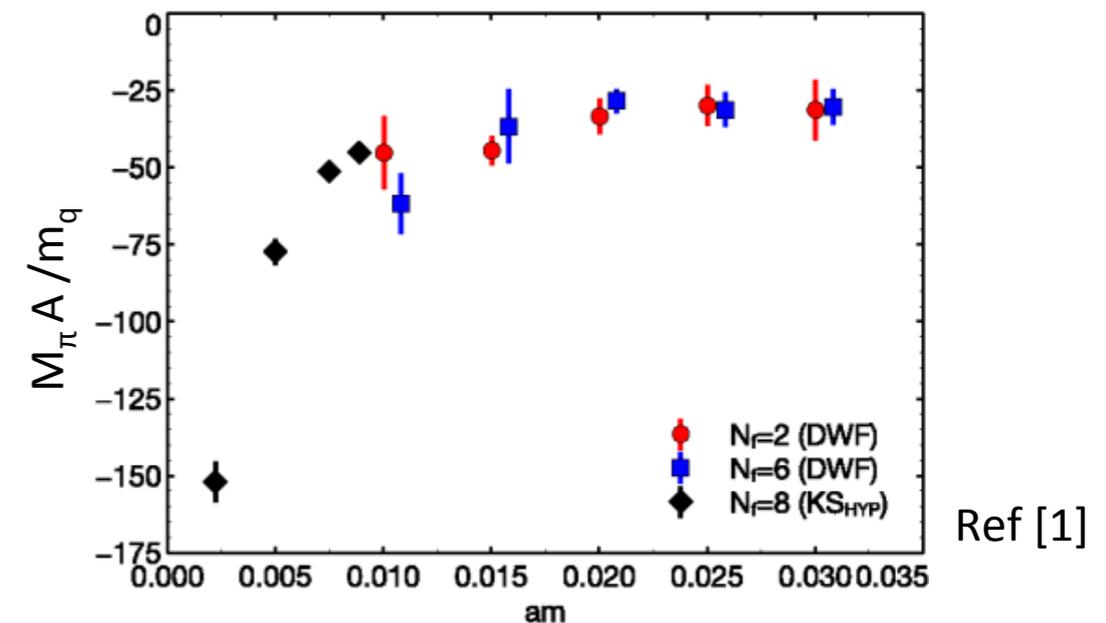
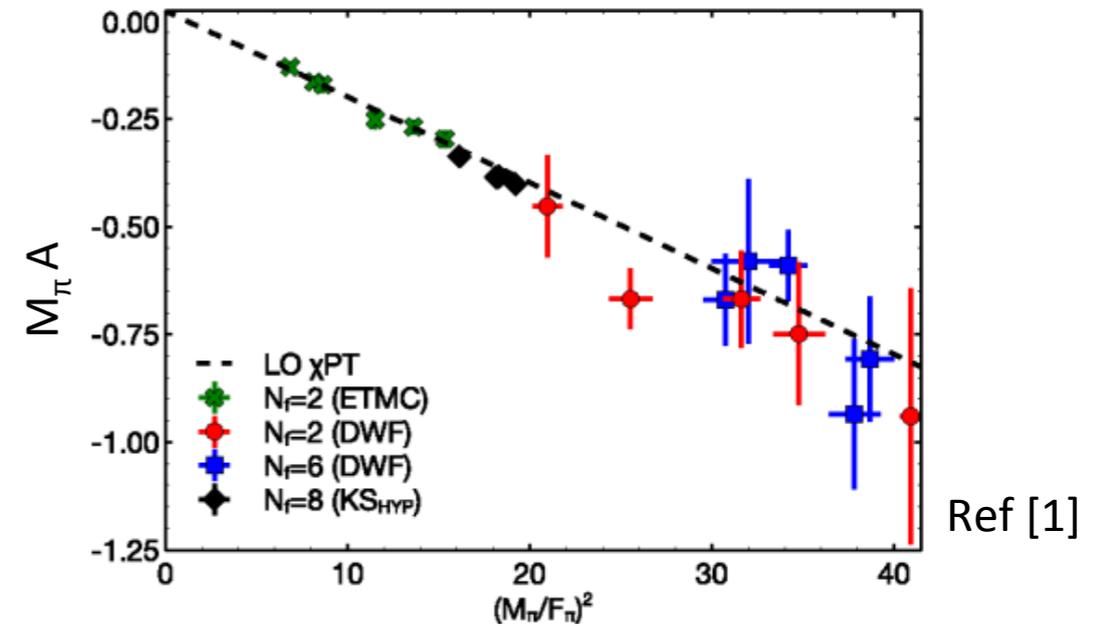
# $I=2$ $\pi\pi$ scattering

## A Clue from Pion Scattering

- Scattering length agrees well with LO XPT when plotted against physical (computed) values of  $M_\pi/F_\pi$ .

$$(M_\pi A)_{LO} = \frac{-1}{(16\pi)^2} \left( \frac{M_\pi}{F_\pi} \right)^2 = \frac{-1}{(16\pi)^2} \frac{2Bm_q}{F^2}$$

- Plotted against bare quark mass, very poor agreement with LO XPT
- Again, suggests  $F$  has significant dependence on chiral breaking at tree level



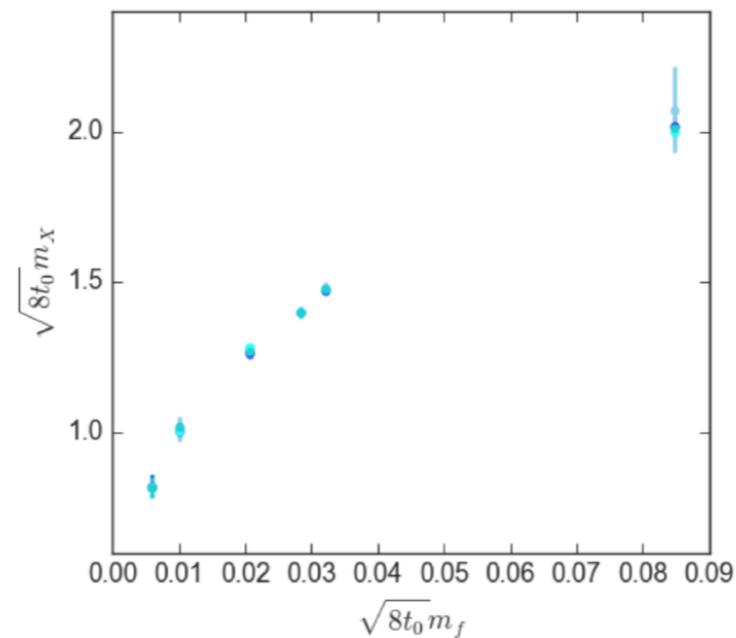
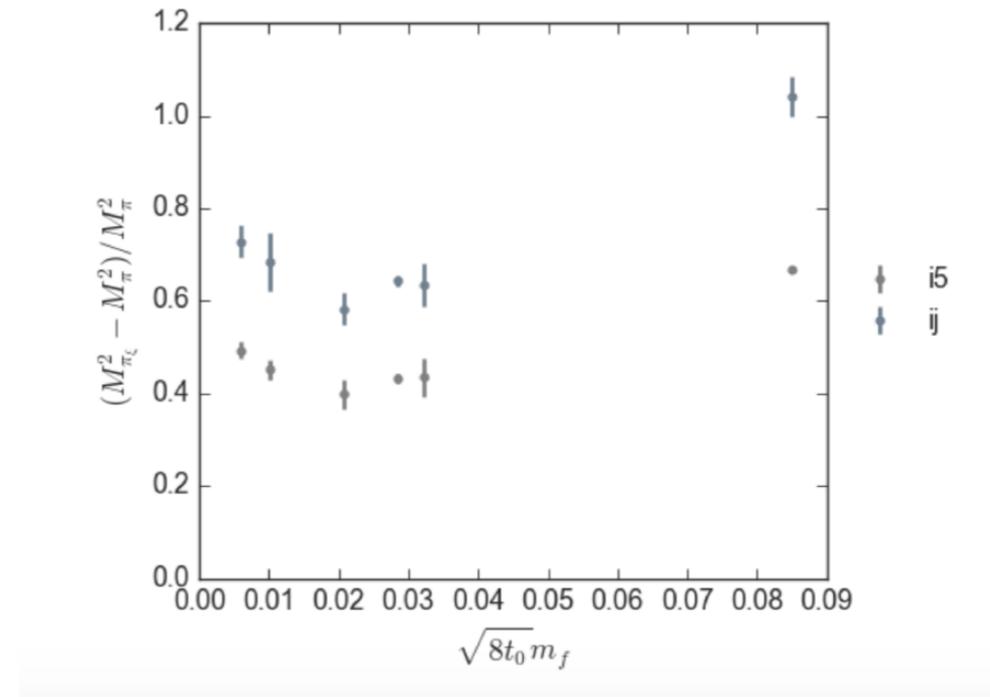
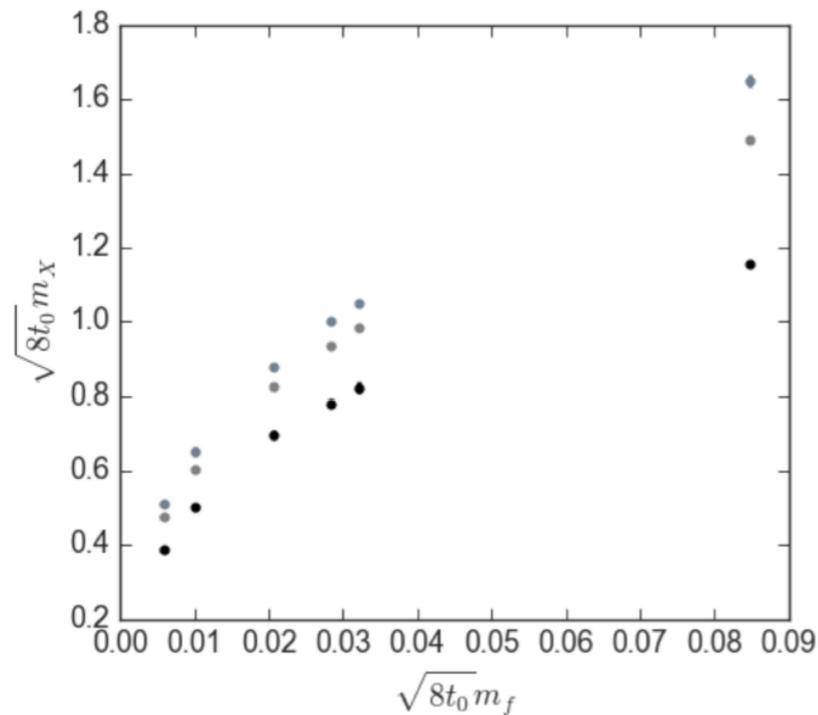
# Finite Volume Effects

- Finite volume effects are small, order 1% in sensitive quantities and order 2% in ratios at  $M_\pi L \sim 5.3$ .
- Note how rapidly quantities change in lattice units with quark mass while ratios change slowly.

$m_f$	volume	$M_\pi$	$F_\pi$	$M_\pi / F_\pi$	$M_\pi L$
0.0075	$24^3 \times 48$	0.21067(19)	0.04746(8)	4.439(9)	5.1
	$32^3 \times 64$	0.20630(6)	0.04823(3)	4.228(3)	6.6
	$48^3 \times 96$	0.20575(3)	0.04827(1)	4.262(1)	9.9
0.005	$32^3 \times 64$	0.16795(10)	0.03939(4)	4.264(6)	5.4
	$48^3 \times 96$	0.16619(7)	0.03996(3)	4.159(4)	8.0
0.00222	$48^3 \times 96$	0.11017(6)	0.02742(3)	4.017(6)	5.3
0.00125	$64^3 \times 128$	0.08273(13)	0.02111(11)	3.918(24)	5.3

# Staggered flavor breaking

- Even though  $a^{-1} \sim 50 F_\pi$  the taste breaking is still rather large. Another consequence of near conformal physics.



# Conclusions

- LSD SU(3)  $N_f=8$  shows evidence of light scalar [pass test 1].
- Lots of evidence for near-conformal dynamics. Is this related to lightness of scalar?
- These data are all preliminary but very close to publication. All lattice ensembles fixed, just analysis.
- We hope these data can be used to shed light on the nature of the EFT for the low energy spectrum.
- Something you didn't see? Ask, and we can show it in discussion.